Discrete Math HW 9: Learning goals N2–N4 due Monday, April 28

*N2: I can compute the greatest common divisor of two natural numbers using the Euclidean Algorithm.* 

**Exercise 1** Use the Euclidean Algorithm to compute each of the following. Be sure to show the steps of the process, not just the final result.

- (a) gcd(1,5)
- (b) gcd(123,277)
- (c) gcd(78, 104)

**Exercise 2** Write a Disco function to find the GCD of two natural numbers using the Euclidean algorithm, by filling in the following template:

gcd : (N \* N) -> N gcd(a,0) = ??? gcd(a,b) = ???

Use your Disco function to find gcd(518303142726377580, 169429189188136020).

*N3: I can compute Bézout coefficients and modular inverses using the Extended Euclidean Algorithm.* 

**Exercise 3** For each pair of numbers *a* and *b*, compute integers *s* and *t* such that sa + tb = gcd(a, b).

- (a) a = 1, b = 5
- (b) *a* = 123, *b* = 277
- (c) a = 78, b = 104

**Exercise 4** For each *a* and *m* below, either find the multiplicative inverse of *a* modulo *m*, or state that it does not have one.

- (a) a = 7, m = 24
- (b) a = 26, m = 39
- (c) *a* = 923, *m* = 77

N4: I can solve modular equivalences in one variable involving addition, subtraction, and multiplication by a constant.

**Exercise 5** Solve each of the following equivalences for *x*. Express your answers in the form  $x \equiv_m r$  where  $0 \le r < m$ .

- (a)  $34x \equiv_{89} 77$
- (b)  $5x + 17 \equiv_{23} 2x 10$
- (c)  $200x 13 \equiv_{1001} 0$

